

A VMS-stabilized mixed formulation for non-linear incompressible solid mechanics problems using the implicit Material Point Method

Laura Moreno¹, Antonia Larese^{1,2}, Alessandro Contri³

¹ Università degli Studi di Padova, Department of Mathematics "Tullio Levi Civita" Torre Archimede, via Trieste 1, 35121, Padova, Italy, laura.morenomartinez@unipd.it

² Technical University of Munich, Germany; Institute for Advanced Study TUM-IAS Lichtenbergstrasse 2 a, D-85748 Garching, Germany

³ Department of Mathematics, NTNU - Norwegian University of Science and Technology, Trondheim, Norway

ABSTRACT

Keywords: *Particle methods, Nonlinear Finite Element Method, Implicit MPM, Mixed formulation, Variational subgrid-scales (VMS), Incompressible solid mechanics*

In our work, two different stabilization techniques, both based on the Variational Multiscale (VMS) method, are employed to solve the dynamic non-linear solid mechanics problem in mixed formulation and in nearly-incompressible conditions.

We use an implicit Material Point Method to deal with large material deformation. This hybrid technique uses a fixed background grid to perform the calculations in a FEM fashion, and a collection of material points (MP) to store all the historical variables. MPM has all the advantage of classical Lagrangian Finite Element formulations, avoiding the need for remeshing.

We propose a Variational Multiscale Stabilization techniques adapted for the implicit MPM mixed UP formulation. VMS method is compared with other stabilization techniques such as the Polynomial Pressure Projection [1], to assess their accuracy.

The proposed mixed formulations are tested through classical benchmarks in solid and geomechanics.

REFERENCES

- [1] Iaconeta I., Larese A., Rossi R. & Oñate E. (2018). A stabilized mixed implicit Material Point Method for non-linear incompressible solid mechanics. *Computational Mechanics*, 1–18.